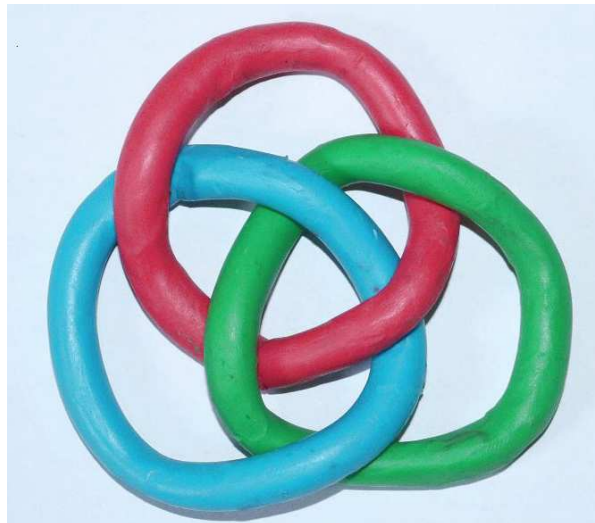


Geometry of Quantum States II

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An Introduction to Quantum Entanglement, 2017

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